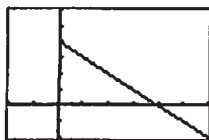


3. Domain of y_1 : $[0, \infty)$; Range of y_1 : $(-\infty, 4]$

y_4 :



$[-2, 6]$ by $[-2, 6]$

$$4. y_3 = y_2(y_1(x)) = \sqrt{y_1(x)} = \sqrt{4-x^2}$$

$$y_4 = y_1(y_2(x)) = 4 - (y_2(x))^2 = 4 - (\sqrt{x})^2 = 4 - x, x \geq 0$$

Quick Review 1.2

1. $3x - 1 \leq 5x + 3$

$$-2x \leq 4$$

$$x \geq -2$$

Solution: $[-2, \infty)$

2. $x(x-2) > 0$

Solutions to $x(x-2) = 0$: $x = 0, x = 2$

Test $x = -1$: $-1(-1-2) = 3 > 0$

$x(x-2) > 0$ is true when $x < 0$.

Test $x = 1$: $1(1-2) = -1 < 0$

$x(x-2) > 0$ is false when $0 < x < 2$.

Test $x = 3$: $3(3-2) = 3 > 0$

$x(x-2) > 0$ is true when $x > 2$.

Solution set: $(-\infty, 0) \cup (2, \infty)$

3. $|x-3| \leq 4$

$$-4 \leq x-3 \leq 4$$

$$-1 \leq x \leq 7$$

Solution set: $[-1, 7]$

4. $|x-2| \geq 5$

$$x-2 \leq -5 \text{ or } x-2 \geq 5$$

$$x \leq -3 \text{ or } x \geq 7$$

Solution set: $(-\infty, -3] \cup [7, \infty)$

5. $x^2 < 16$

Solution to $x^2 = 16$: $x = -4, x = 4$

Test $x = -6$: $(-6)^2 = 36 > 16$

$x^2 < 16$ is false when $x < -4$

Test $x = 0$: $0^2 = 0 < 16$

$x^2 < 16$ is true when $-4 < x < 4$

Test $x = 6$: $6^2 = 36 > 16$

$x^2 < 16$ is false when $x > 4$.

Solution set: $(-4, 4)$

6. $9 - x^2 \geq 0$

Solutions to $9 - x^2 = 0$: $x = -3, x = 3$

Test $x = -4$: $9 - (-4)^2 = 9 - 16 = -7 < 0$

$9 - x^2 \geq 0$ is false when $x < -3$.

Test $x = 0$: $9 - 0^2 = 9 > 0$

$9 - x^2 \geq 0$ is true when $-3 < x < 3$.

Test $x = 4$: $9 - 4^2 = 9 - 16 = -7 < 0$

$9 - x^2 \geq 0$ is false when $x > 3$.

Solution set: $[-3, 3]$

7. Translate the graph of f 2 units left and 3 units downward.

8. Translate the graph of f 5 units right and 2 units upward.

9. (a) $f(x) = 4$

$$x^2 - 5 = 4$$

$$x^2 - 9 = 0$$

$$(x+3)(x-3) = 0$$

$$x = -3 \text{ or } x = 3$$

(b) $f(x) = -6$

$$x^2 - 5 = -6$$

$$x^2 = -1$$

No real solution

10. (a) $f(x) = -5$

$$\frac{1}{x} = -5$$

$$x = -\frac{1}{5}$$

(b) $f(x) = 0$

$$\frac{1}{x} = 0$$

No solution

11. (a) $f(x) = 4$

$$\sqrt{x+7} = 4$$

$$x+7 = 16$$

$$x = 9$$

Check: $\sqrt{9+7} = \sqrt{16} = 4$; it checks.

(b) $f(x) = 1$

$$\sqrt{x+7} = 1$$

$$x+7 = 1$$

$$x = -6$$

Check: $\sqrt{-6+7} = 1$; it checks.

12. (a) $f(x) = -2$

$$\sqrt[3]{x-1} = -2$$

$$x-1 = -8$$

$$x = -7$$

(b) $f(x) = 3$

$$\sqrt[3]{x-1} = 3$$

$$x-1 = 27$$

$$x = 28$$

Section 1.2 Exercises

1. $A(d) = \pi \left(\frac{d}{2}\right)^2$
 $A(d) = \pi \left(\frac{4 \text{ in}}{2}\right)^2 = \pi(2 \text{ in})^2 = 4\pi \text{ in}^2$

2. $h(s) = \frac{\sqrt{3}}{2}s = 3\frac{\sqrt{3}}{2}m = 1.5\sqrt{3}m$

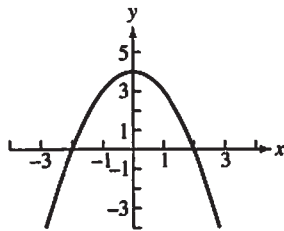
3. $S(e) = 6e^2 = 6(5 \text{ ft})^2 = 6(25 \text{ ft}^2) = 150 \text{ ft}^2$

4. $v(r) = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi(3 \text{ cm})^3$
 $= \frac{4}{3}\pi(27 \text{ cm}^3) = 36\pi \text{ cm}^3$

5. (a) $(-\infty, \infty)$ or all real numbers

(b) $(-\infty, 4]$

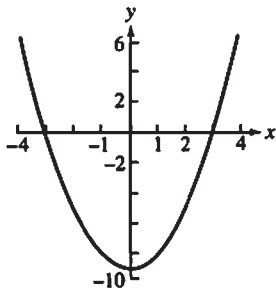
(c)



6. (a) $(-\infty, \infty)$ or all real numbers

(b) $[-9, \infty)$

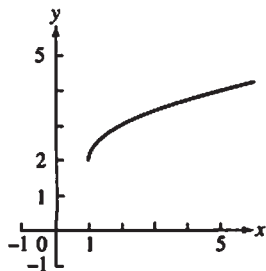
(c)



7. (a) Since we require $x - 1 \geq 0$, the domain is $[1, \infty)$.

(b) $[2, \infty)$

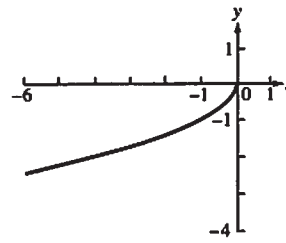
(c)



8. (a) Since we require $-x \geq 0$, the domain is $(-\infty, 0]$.

(b) $(-\infty, 0]$

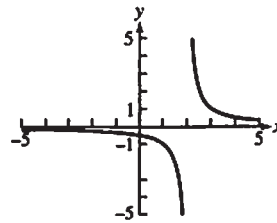
(c)



9. (a) Since we require $x - 2 \neq 0$, the domain is $(-\infty, 2) \cup (2, \infty)$.

(b) Since $\frac{1}{x-2}$ can assume any value except 0, the range is $(-\infty, 0) \cup (0, \infty)$.

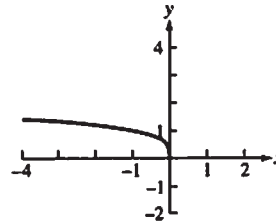
(c)



10. (a) Since we require $-x \geq 0$, the domain is $(-\infty, 0]$.

(b) $[0, \infty)$

(c)

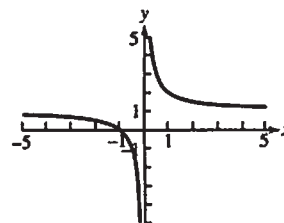


11. (a) Since we require $x \neq 0$, the domain is $(-\infty, 0) \cup (0, \infty)$.

(b) Note that $\frac{1}{x}$ can assume any value except 0, so $1 + \frac{1}{x}$ can assume any value except 1.

The range is $(-\infty, 1) \cup (1, \infty)$.

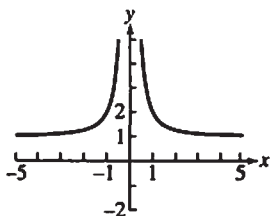
(c)



12. (a) Since we require $x^2 \neq 0$, the domain is $(-\infty, 0) \cup (0, \infty)$

(b) Since $\frac{1}{x^2} > 0$ for all x , the range is $(0, \infty)$.

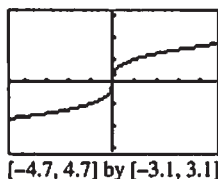
(c)



13. (a) $(-\infty, \infty)$ or all real numbers

(b) $(-\infty, \infty)$ or all real numbers

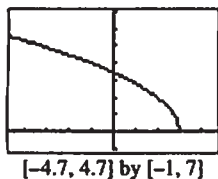
(c)



14. (a) Since we require $3 - x \geq 0$, the domain is $(-\infty, 3]$.

(b) $[0, \infty)$

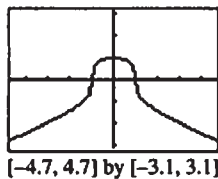
(c)



15. (a) $(-\infty, \infty)$ or all real numbers

(b) The maximum function value is attained at the point $(0, 1)$, so the range is $(-\infty, 1]$.

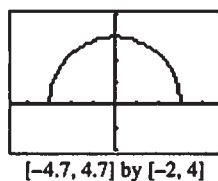
(c)



16. (a) Since we require $9 - x^2 \geq 0$ the domain is $[-3, 3]$

(b) $[0, 3]$

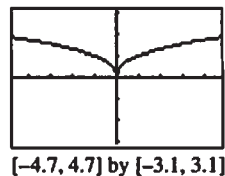
(c)



17. (a) $(-\infty, \infty)$ or all real numbers

(b) Since $x^{2/5}$ is equivalent to $\sqrt[5]{x^2}$, the range is $[0, \infty)$

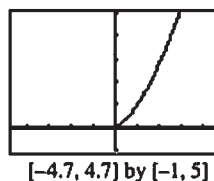
(c)



18. (a) This function is equivalent to $y = \sqrt{x^3}$, so its domain is $[0, \infty)$.

(b) $[0, \infty)$

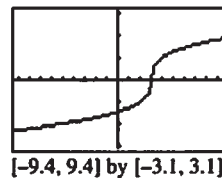
(c)



19. (a) $(-\infty, \infty)$ or all real numbers

(b) $(-\infty, \infty)$ or all real numbers

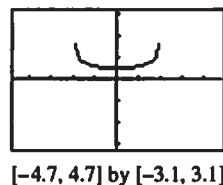
(c)



20. (a) Since $(4 - x^2) > 0$, the domain is $(-2, 2)$

(b) $[0.5, \infty)$

(c)



21. Even, since the function is an even power of x .

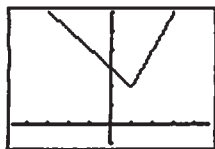
22. Neither, since the function is a sum of even and odd powers of x .

23. Neither, since the function is a sum of even and odd powers of $x(x^1 + 2x^0)$.

24. Even, since the function is a sum of even powers of $x(x^2 - 3x^0)$.

25. Even, since the function involves only even powers of x .
26. Odd, since the function is a sum of odd powers of x .
27. Odd, since the function is a quotient of an odd function (x^3) and an even function ($x^2 - 1$).
28. Neither, since, (for example), $y(-2) = 4^{1/3}$ and $y(2) = 0$.
29. Neither, since, (for example), $y(-1)$ is defined and $y(1)$ is undefined.
30. Even, since the function involves only even powers of x .

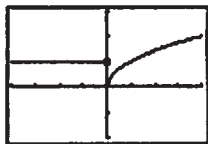
31. (a)



[-4.7, 4.7] by [-1, 6]

(b) $(-\infty, \infty)$ or all real numbers(c) $[2, \infty)$

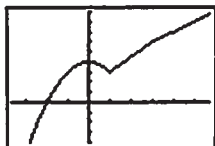
32. (a)



[-4, 4] by [-2, 3]

(b) $(-\infty, \infty)$ or all real numbers(c) $[0, \infty)$

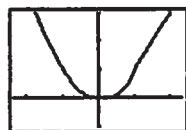
33. (a)



[-3.7, 5.7] by [-4, 9]

(b) $(-\infty, \infty)$ or all real numbers(c) $(-\infty, \infty)$ or all real numbers

34. (a)



[-2.35, 2.35] by [-1, 3]

(b) $(-\infty, \infty)$ or all real numbers(c) $[0, \infty)$

35. Because if the vertical line test holds, then for each x -coordinate, there is at most one y -coordinate giving a point on the curve. This y -coordinate would correspond to the value assigned to the x -coordinate. Since there is only one y -coordinate, the assignment would be unique.

36. If the curve is not $y = 0$, there must be a point (x, y) on the curve where $y \neq 0$. That would mean that (x, y) and $(x, -y)$ are two different points on the curve and it is not the graph of a function, since it fails the vertical line test.

37. No

38. Yes

39. Yes

40. No

41. Line through $(0, 0)$ and $(1, 1)$: $y = x$ Line through $(1, 1)$ and $(2, 0)$: $y = -x + 2$

$$f(x) = \begin{cases} x, & 0 \leq x \leq 1 \\ -x + 2, & 1 < x \leq 2 \end{cases}$$

$$42. f(x) = \begin{cases} 2, & 0 \leq x < 1 \\ 0, & 1 \leq x < 2 \\ 2, & 2 \leq x < 3 \\ 0, & 3 \leq x \leq 4 \end{cases}$$

43. Line through $(0, 2)$ and $(2, 0)$: $y = -x + 2$ Line through $(2, 1)$ and $(5, 0)$: $m = \frac{0-1}{5-2} = \frac{-1}{3} = -\frac{1}{3}$,

$$\text{so } y = -\frac{1}{3}(x-2) + 1 = -\frac{1}{3}x + \frac{5}{3}$$

$$f(x) = \begin{cases} -x + 2, & 0 < x \leq 2 \\ -\frac{1}{3}x + \frac{5}{3}, & 2 < x \leq 5 \end{cases}$$

44. Line through $(-1, 0)$ and $(0, -3)$:

$$m = \frac{-3-0}{0-(-1)} = \frac{-3}{1} = -3, \text{ so } y = -3x - 3$$

Line through $(0, 3)$ and $(2, -1)$:

$$m = \frac{-1-3}{2-0} = \frac{-4}{2} = -2, \text{ so } y = -2x + 3$$

$$f(x) = \begin{cases} -3x - 3, & -1 < x \leq 0 \\ -2x + 3, & 0 < x \leq 2 \end{cases}$$

45. Line through $(-1, 1)$ and $(0, 0)$: $y = -x$
 Line through $(0, 1)$ and $(1, 1)$: $y = 1$
 Line through $(1, 1)$ and $(3, 0)$:

$$m = \frac{0-1}{3-1} = \frac{-1}{2} = -\frac{1}{2},$$

$$\text{so } y = -\frac{1}{2}(x-1) + 1 = -\frac{1}{2}x + \frac{3}{2}$$

$$f(x) = \begin{cases} -x, & -1 \leq x < 0 \\ 1, & 0 < x \leq 1 \\ -\frac{1}{2}x + \frac{3}{2}, & 1 < x < 3 \end{cases}$$

46. Line through $(-2, -1)$ and $(0, 0)$: $y = \frac{1}{2}x$

Line through $(0, 2)$ and $(1, 0)$: $y = -2x + 2$

Line through $(1, -1)$ and $(3, -1)$: $y = -1$

$$f(x) = \begin{cases} \frac{1}{2}x, & -2 \leq x \leq 0 \\ -2x + 2, & 0 < x \leq 1 \\ -1, & 1 < x \leq 3 \end{cases}$$

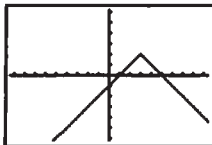
47. Line through $(\frac{T}{2}, 0)$ and $(T, 1)$:

$$m = \frac{1-0}{T-(T/2)} = \frac{2}{T}, \text{ so } y = \frac{2}{T}\left(x - \frac{T}{2}\right) + 0 = \frac{2}{T}x - 1$$

$$f(x) = \begin{cases} 0, & 0 \leq x \leq \frac{T}{2} \\ \frac{2}{T}x - 1, & \frac{T}{2} < x \leq T \end{cases}$$

$$48. f(x) = \begin{cases} A, & 0 \leq x < \frac{T}{2} \\ -A, & \frac{T}{2} \leq x < T \\ A, & T \leq x < \frac{3T}{2} \\ -A, & \frac{3T}{2} \leq x \leq 2T \end{cases}$$

49. (a)

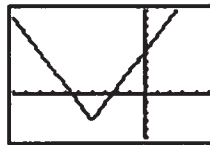


$[-9.4, 9.4]$ by $[-6.2, 6.2]$

Note that $f(x) = -|x-3| + 2$, so its graph is the graph of the absolute value function reflected across the x -axis and then shifted 3 units right and 2 units upward.

- (b) $(-\infty, \infty)$
 (c) $(-\infty, 2]$

50. (a) The graph of $f(x)$ is the graph of the absolute value function stretched vertically by a factor of 2 and then shifted 4 units to the left and 3 units downward.



$[-10, 5]$ by $[-5, 10]$

- (b) $(-\infty, \infty)$ or all real numbers
 (c) $[-3, \infty)$
51. (a) $f(g(x)) = (x^2 - 3) + 5 = x^2 + 2$
 (b) $g(f(x)) = (x+5)^2 - 3 = (x^2 + 10x + 25) - 3 = x^2 + 10x + 22$
 (c) $f(g(0)) = 0^2 + 2 = 2$
 (d) $g(f(0)) = 0^2 + 10 \cdot 0 + 22 = 22$
 (e) $g(g(-2)) = [(-2)^2 - 3]^2 - 3 = 1^2 - 3 = -2$
 (f) $f(f(x)) = (x+5) + 5 = x + 10$
52. (a) $f(g(x)) = (x-1) + 1 = x$
 (b) $g(f(x)) = (x+1) - 1 = x$
 (c) $f(g(x)) = 0$
 (d) $g(f(0)) = 0$
 (e) $g(g(-2)) = (-2-1) - 1 = -3 - 1 = -4$
 (f) $f(f(x)) = (x+1) + 1 = x + 2$

53. (a) Since $(f \circ g)(x) = \sqrt{g(x)-5} = \sqrt{x^2-5}$, $g(x) = x^2$.

- (b) Since $(f \circ g)(x) = 1 + \frac{1}{g(x)} = x$, we know that

$$\frac{1}{g(x)} = x - 1, \text{ so } g(x) = \frac{1}{x-1}.$$

- (c) Since $(f \circ g)(x) = f\left(\frac{1}{x}\right) = x$, $f(x) = \frac{1}{x}$.

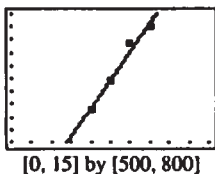
- (d) Since $(f \circ g)(x) = f(\sqrt{x}) = |x|$, $f(x) = x^2$.

The completed table is shown. Note that the absolute value sign in part (d) is optional.

$g(x)$	$f(x)$	$(f \circ g)(x)$
x^2	$\sqrt{x-5}$	$\sqrt{x^2-5}$
$\frac{1}{x-1}$	$1 + \frac{1}{x}$	$x, x \neq -1$
$\frac{1}{x}$	$\frac{1}{x}$	$x, x \neq 0$
\sqrt{x}	x^2	$ x , x \geq 0$

54. (a) $y = 2.893x^2 - 24.107x + 590.214$

(b)



(c) $y = 2.893(18)^2 - 24.107(18) + 590.214$
 $= 937.332 - 433.926 + 590.214$
 $= \$1093 \text{ million or } \1.093 billion

(d) linear regression: $y = 33.75x + 312.5$

$y = 33.75(18) + 312.5 = \$920 \text{ million in } 2008.$

55. (a) Because the circumference of the original circle was 8π and a piece of length x was removed.

(b) $r = \frac{8\pi - x}{2\pi} = 4 - \frac{x}{2\pi}$

(c) $h = \sqrt{16 - r^2}$
 $= \sqrt{16 - \left(4 - \frac{x}{2\pi}\right)^2}$
 $= \sqrt{16 - \left(16 - \frac{4x}{\pi} + \frac{x^2}{4\pi^2}\right)}$
 $= \sqrt{\frac{4x}{\pi} - \frac{x^2}{4\pi^2}}$
 $= \sqrt{\frac{16\pi x}{4\pi^2} - \frac{x^2}{4\pi^2}}$
 $= \frac{\sqrt{16\pi x - x^2}}{2\pi}$

(d) $V = \frac{1}{3}\pi r^2 h$
 $= \frac{1}{3}\pi \left(\frac{8\pi - x}{2\pi}\right)^2 \cdot \frac{\sqrt{16\pi x - x^2}}{2\pi}$
 $= \frac{(8\pi - x)^2 \sqrt{16\pi x - x^2}}{24\pi^2}$

56. (a) Note that 2 mi = 10,560 ft, so there are $\sqrt{800^2 + x^2}$ feet of river cable at \$180 per foot and $(10,560 - x)$ feet of land cable at \$100 per foot. The cost is

$C(x) = 180\sqrt{800^2 + x^2} + 100(10,560 - x)$

(b) $C(0) = \$1,200,000$
 $C(500) \approx \$1,175,812$
 $C(1000) \approx \$1,186,512$
 $C(1500) \approx \$1,212,000$
 $C(2000) \approx \$1,243,732$
 $C(2500) \approx \$1,278,479$
 $C(3000) \approx \$1,314,870$

Values beyond this are all larger. It would appear that the least expensive location is less than 2000 ft from point P.

57. False: $x^4 + x^2 + x \neq (-x)^4 + (-x)^2 + (-x).$

58. True: $(-x)^3 = -x^3$

59. B: Since $9 - x^2 > 0$, the domain is $(-3, 3)$

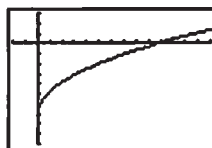
60. A: $y \neq 1$

61. D: $(f \circ g)(2) = f(x+3)(2) = 2(x+3) - 1$
 $= 2(2+3) - 1 = 2(5) - 1 = 10 - 1 = 9$

62. C: $A(w) = Lw$
 $L = 2w$
 $A(w) = 2w^2$

63. (a) Enter $y_1 = f(x) = x - 7, y_2 = g(x) = \sqrt{x},$
 $y_3 = (f \circ g)(x) = y_1(y_2(x)),$ and
 $y_4 = (g \circ f)(x) = y_2(y_1(x))$

$f \circ g:$

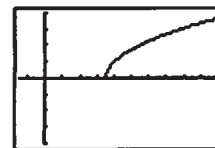


$[-10, 70]$ by $[-10, 3]$

Domain: $[0, \infty)$

Range: $[-7, \infty)$

$g \circ f:$



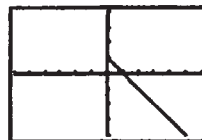
$[-3, 20]$ by $[-4, 4]$

Domain: $[7, \infty)$

Range: $[0, \infty)$

(b) $(f \circ g)(x) = \sqrt{x} - 7$ $(g \circ f)(x) = \sqrt{x - 7}$

64. (a) Enter $y_1 = f(x) = 1 - x^2, y_2 = g(x) = \sqrt{x},$
 $y_3 = (f \circ g)(x) = y_1(y_2(x)),$ and $y_4 = (g \circ f)(x)$
 $= y_2(y_1(x))$
 $f \circ g:$

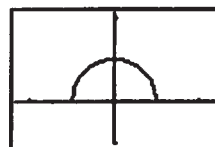


$[-6, 6]$ by $[-4, 4]$

Domain: $[0, \infty)$

Range: $(-\infty, 1]$

$g \circ f:$



$[-2.35, 2.35]$ by $[-1, 2.1]$

Domain: $[-1, 1]$

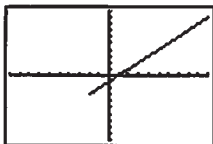
Range: $[0, 1]$

(b) $(f \circ g)(x) = 1 - (\sqrt{x})^2 = 1 - x, x \geq 0$
 $(g \circ f)(x) = \sqrt{1 - x^2}$

65. (a) Enter $y_1 = f(x) = x^2 - 3$, $y_2 = g(x) = \sqrt{x+2}$,

$$y_3 = (f \circ g)(x) = y_1(y_2(x)), \text{ and } y_4 = (g \circ f)(x) = y_2(y_1(x)).$$

$f \circ g$:

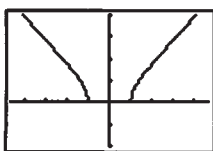


$[-10, 10]$ by $[-10, 10]$

Domain: $[-2, \infty)$

Range: $[-3, \infty)$

$g \circ f$:



$[-4.7, 4.7]$ by $[-2, 4]$

Domain: $(-\infty, -1] \cup [1, \infty)$

Range: $[0, \infty)$

(b) $(f \circ g)(x) = (\sqrt{x+2})^2 - 3 = (x+2) - 3, x \geq -2 = x - 1, x \geq -2$

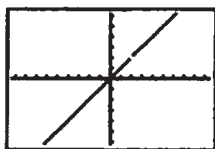
$$(g \circ f)(x) = \sqrt{(x^2 - 3) + 2} = \sqrt{x^2 - 1}$$

66. (a) Enter $y_1(x) = f(x) = \frac{2x-1}{x+3}$, $y_2 = \frac{3x+1}{2-x}$,

$$y_3 = (f \circ g)(x) = y_1(y_2(x)), \text{ and } y_4 = (g \circ f)(x) = y_2(y_1(x)).$$

Use a "decimal window" such as the one shown.

$f \circ g$:

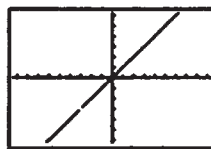


$[-9.4, 9.4]$ by $[-6.2, 6.2]$

Domain: $(-\infty, 2) \cup (2, \infty)$

Range: $(-\infty, 2) \cup (2, \infty)$

$g \circ f$:



$[-9.4, 9.4]$ by $[-6.2, 6.2]$

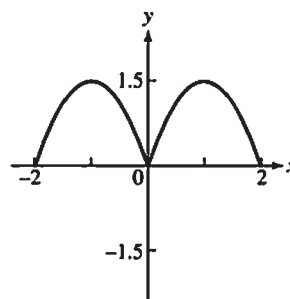
Domain: $(-\infty, -3) \cup (-3, \infty)$

Range: $(-\infty, -3) \cup (-3, \infty)$

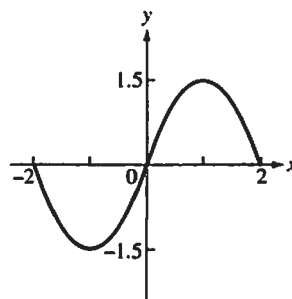
$$\begin{aligned} \text{(b) } (f \circ g)(x) &= \frac{2\left(\frac{3x+1}{2-x}\right) - 1}{\frac{3x+1}{2-x} + 3} \\ &= \frac{2(3x+1) - (2-x)}{(3x+1) + 3(2-x)}, x \neq 2 \\ &= \frac{7x}{7}, x \neq 2 \\ &= x, x \neq 2 \end{aligned}$$

$$\begin{aligned} (g \circ f)(x) &= \frac{3\left(\frac{2x-1}{x+3}\right) + 1}{2 - \frac{2x-1}{x+3}} \\ &= \frac{3(2x-1) + (x+3)}{2(x+3) - (2x-1)}, x \neq -3 \\ &= \frac{7x}{7}, x \neq -3 \\ &= x, x \neq -3 \end{aligned}$$

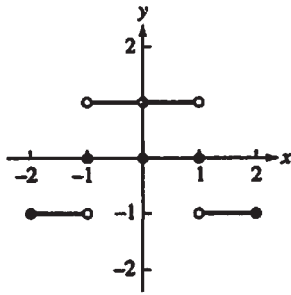
67. (a)



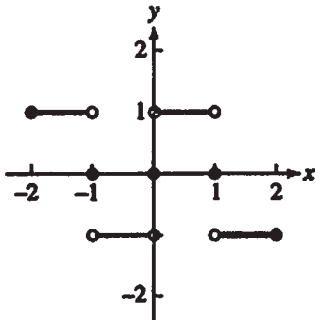
(b)



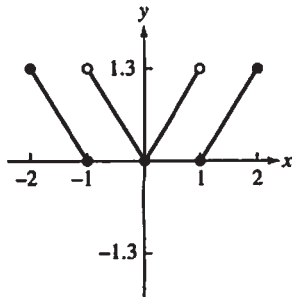
68. (a)



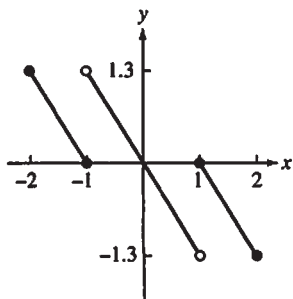
(b)



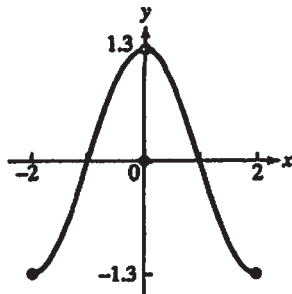
69. (a)



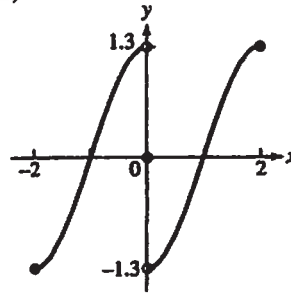
(b)



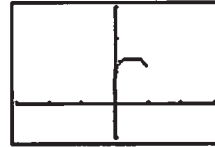
70. (a)



(b)



71. (a)



$[-3, 3]$ by $[-1, 3]$

(b) Domain of y_1 : $[0, \infty)$

Domain of y_2 : $(-\infty, 1]$

Domain of y_3 : $[0, 1]$

(c) The functions $y_1 - y_2$, $y_2 - y_1$, and $y_1 \cdot y_2$ all have domain $[0, 1]$, the same as the domain of $y_1 + y_2$ found in part (b).

Domain of $\frac{y_1}{y_2}$: $(0, 1)$

Domain of $\frac{y_2}{y_1}$: $(0, 1)$

(d) The domain of a sum, difference, or product of two functions is the intersection of their domains. The domain of a quotient of two functions is the intersection of their domains with any zeros of the denominator removed.

72. (a) Yes. Since

$$(f \circ g)(-x) = f(-x) \circ g(-x) = f(x) \circ g(x) = (f \circ g)(x),$$

the function $(f \circ g)(x)$ will also be even.

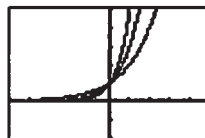
(b) The product will be even, since

$$\begin{aligned} (f \circ g)(-x) &= f(-x) \circ g(-x) \\ &= (-f(x)) \circ (-g(x)) \\ &= f(x) \circ g(x) \\ &= (f \circ g)(x). \end{aligned}$$

Section 1.3 Exponential Functions (pp. 22–29)

Exploration 1 Exponential Functions

1.



$[-5, 5]$ by $[-2, 5]$

2. $x > 0$

3. $x < 0$

4. $x = 0$

5.



[-5, 5] by [-2, 5]

6. $2^{-x} < 3^{-x} < 5^{-x}$ for $x < 0$; $2^{-x} > 3^{-x} > 5^{-x}$ for $x > 0$; $2^{-x} = 3^{-x} = 5^{-x}$ for $x = 0$.

Quick Review 1.3

1. Using a calculator, $5^{2/3} \approx 2.924$.

2. Using a calculator, $3^{\sqrt{2}} \approx 4.729$.

3. Using a calculator, $3^{-1.5} \approx 0.192$.

4. $x^3 = 17$

$x = \sqrt[3]{17}$

$x \approx 2.5713$

5. $x^5 = 24$

$x = \sqrt[5]{24}$

$x \approx 1.8882$

6. $x^{10} = 1.4567$

$x = \pm \sqrt[10]{1.4567}$

$x \approx \pm 1.0383$

7. $500(1.0475)^5 \approx \$630.58$

8. $1000(1.063)^3 \approx \$1201.16$

$$9. \frac{(x^{-3}y^2)^2}{(x^4y^3)^3} = \frac{x^{-6}y^4}{x^{12}y^9}$$

$$= x^{-6-12}y^{4-9}$$

$$= x^{-18}y^{-5}$$

$$= \frac{1}{x^{18}y^5}$$

$$10. \left(\frac{a^3b^{-2}}{c^4}\right)^2 \left(\frac{a^4c^{-2}}{b^3}\right)^{-1} = \frac{a^6b^{-4}}{c^8} \cdot \frac{b^3}{a^4c^{-2}}$$

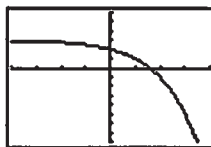
$$= \frac{a^6}{b^4c^8} \cdot \frac{b^3c^2}{a^4}$$

$$= a^{6-4}b^{-4+3}c^{-8+2}$$

$$= a^2b^{-1}c^{-6} = \frac{a^2}{bc^6}$$

Section 1.3 Exercises

1.



[-4, 4] by [-8, 6]

Domain: $(-\infty, \infty)$ Range: $(-\infty, 3)$

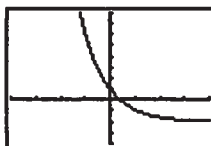
2.



[-4, 4] by [-2, 10]

Domain: $(-\infty, \infty)$ Range: $(3, \infty)$

3.



[-4, 4] by [-4, 8]

Domain: $(-\infty, \infty)$ Range: $(-2, \infty)$

4.



[-4, 4] by [-8, 4]

Domain: $(-\infty, \infty)$ Range: $(-\infty, -1)$

5. $9^{2x} = (3^2)^{2x} = 3^{4x}$

6. $16^{3x} = (2^4)^{3x} = 2^{12x}$

7. $\left(\frac{1}{8}\right)^{2x} = (2^{-3})^{2x} = 2^{-6x}$

8. $\left(\frac{1}{27}\right)^x = (3^{-3})^x = 3^{-3x}$

9. x -intercept: ≈ -2.322

y -intercept: -4.0

10. x -intercept: ≈ 1.386

y -intercept: -3.0